

Fourier integral (Fourier transform)

1) General Information

Decomposition of a continuous aperiodic signal to a continuous spectrum.

Advantages: Simplification of mathematical calculations for example convolution and multiplication.

2) Components of the formulas

$$U(f) = \int_{-\infty}^{\infty} u(t) \cdot e^{-j2\pi ft} dt \quad \text{Fourier transform}$$

$$u(t) = \int_{-\infty}^{\infty} U(f) \cdot e^{+j2\pi ft} df \quad \text{Inverse transform}$$

$U(f)$ $\hat{=}$ Spectral amplitude density

$u(t)$ $\hat{=}$ Signal, time domain of the function

with: $u, U \in \mathbb{C}$
 $t, f \in \mathbb{R}$

dt $\hat{=}$ Integration over a time variable

df $\hat{=}$ Integration over a frequency variable

$e^{-j2\pi ft}$ $\hat{=}$ Kernel function

$$\hookrightarrow e^{jx} = \cos(x) + j \cdot \sin(x)$$

$$e^{-jx} = \cos(x) - j \cdot \sin(x)$$

Description of an aperiodic signal with infinite sine- and cosine-oscillations